

Statistics 201 Exam 2 – Practice Exam
Spring 2024
Chapters 07 – Sampling Distributions

Disclaimer:

This practice exam is provided solely for the purpose of familiarizing you with the format and style of the Stat 201 exams. There is no explicit or implicit guarantee that the upcoming exam will ask similar questions. If you use the practice exam as your only tool to help you prepare for the upcoming exam, you most likely will not do well on the exam. You should still do the things you would have done if you did not have access to this practice exam, such as re-read the text, go over your class notes, re-work the online homework problems, and look at the list of exam topics provided and make sure that you understand all the concepts listed within it.

NOTE: These questions come from actual older exams. As such, the points on this practice exam may total more than 100 points.

The logo for Haslam College of Business is centered on a light blue rectangular background. It features the word "HASLAM" in large, bold, orange, sans-serif capital letters. Below it, the words "COLLEGE OF BUSINESS" are written in a smaller, bold, orange, sans-serif font. At the bottom, "THE UNIVERSITY OF TENNESSEE, KNOXVILLE" is written in a smaller, dark grey, serif font.

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Exam Grade: _____

1. Say we have a fair (two-sided) coin which we will flip.

i) (2 points) If the first three coin flips come up tails, what is the probability that the fourth coin flip comes up tails?

ii) (2 points) What is the probability of getting five tails in a row?

2. Suppose we have two events A and B with $P(A)=.3$ and $P(B)=.5$.

i) (3 points) Find $P(A \text{ or } B)$, assuming A and B are disjoint (i.e., mutually exclusive).

ii) (3 points) Find $P(A \text{ and } B)$, assuming A and B are independent.

3. (3 points) Suppose we are considering a person's drive to work one day. Let Event C represent this person being rear-ended by another vehicle before they get to work. Let event D represent this person getting to work without having any sort collision with anything. Let's assume the following:

$$P(C) = 0.0002$$

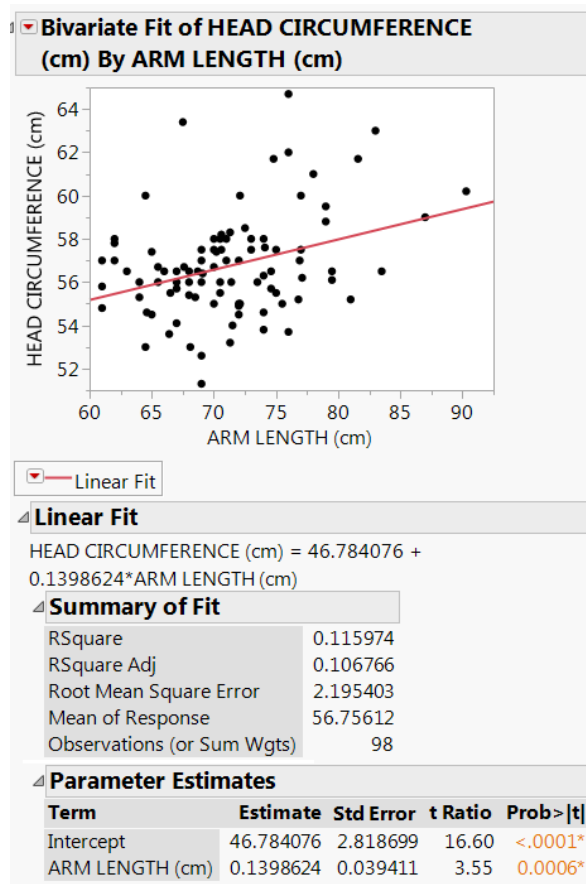
$$P(D) = 0.9995$$

Find $P(C \text{ and } D)$.

4. In Stat 201, a group of students measured their head circumference and their right arm length. Below is some output from JMP for a regression analysis, using:

X = right arm length (cm)

Y = head circumference (cm):



- i) (1 point) Based on the output above, is the linear relationship between these two variables “statistically significant”? Circle one: YES NO
- ii) (2 points) Circle the ONE value in the output that lead to your conclusion in part (i).
- iii) (3 points) Regardless of your answers above, briefly describe what it means for a linear relationship to be “statistically significant”. Limit your answer to two or less sentences.

5. The following regression equation was developed after a large number of nursing students agreed to share their latest medical records with us:

$$\text{Height (in.)} = 54.55 + 0.085 * \text{Weight (lbs.)}$$

- i) (2 points) Mary was one of the nursing students that were part of this study. Suppose Mary weighs 110 pounds. Use the regression equation above to predict Mary's height (in inches).
- ii) (2 points) If Mary is actually 65 inches tall, what would the residual for this observation be? [Note: if you have no answer for part (i), use 60.4 inches, which is NOT the correct answer for part (i).]
- iii) (3 points) Interpret the slope of this regression equation in the context of this problem.
- iv) (4 points) John, another nursing student that was part of this study, is 68 inches tall. We used the above regression equation to find John's predicted height, and then calculated the residual for this observation, and found that the residual was -1.47. How much does John weigh (in pounds)?

6. A major airline wants to find out if additional charges for baggage affects the airline passengers choose to fly with and how often they fly. They decide to survey passengers who are flying on their airline.

i) (3 points) The airline decides to randomly select 30 of their flights over a one week period and survey all passengers on those flights. What sampling method is being used?

- a) Simple Random Sample
- b) Convenience
- c) Cluster
- d) Systematic
- e) Stratified

ii) (3 points) What is the sampling frame?

- a) All passengers that fly on any airline.
- b) All passengers that fly this particular airline.
- c) All passengers that flew this particular airline during the week they did the survey.
- d) All passengers on the 30 randomly selected flights.
- e) All passengers that chose to participate in the survey.

iii) (4 points) Explain one potential source of bias using this sampling method.

iv) (3 points) Suppose instead that the airline decides to survey passengers on all of its flights on a single day by selecting every 10th passenger entering each of its planes to take the survey. What sampling method is being used?

- a) Simple Random Sample
- b) Convenience
- c) Cluster
- d) Systematic
- e) Stratified

7. (5 points) A high school student is interested in attending an “Ivy League” school. As long as a student has a high school GPA of 4.0 and an SAT score of at least 1300, there is a 38% chance of getting accepted to any one of these institutions. One can assume that being accepted or rejected is independent across the eight Ivy League colleges.

What is the probability that this student is accepted to at least one of these schools, provided the student has met the acceptance requirements and the GPA and SAT criteria described above?

8. The owner of a new apartment building must install 50 water heaters. Let's say that the proportion of all Always Hot brand water heaters that will last 10 or more years is 0.25. We can think of the 50 Always Hot brand water heaters that this owner actually buys as a random sample from all Always Hot brand water heaters. After 10 years go by, the owner will know the proportion of water heaters (out of the 50 she purchased) that actually lasted 10 years. This proportion can be thought of as a "sample proportion".

i) (3 points) In this example, the "sampling distribution of the sample proportion" refers to (circle the best answer):

- a) The distribution of all possible sample proportions from samples of size $n=50$.
- b) The exact value of the sample proportion this owner will calculate.
- c) The distribution of all possible sample proportions for all possible sample sizes.
- d) The exact value of the population proportion.
- e) The distribution of the population proportion.

ii) (6 points) To be able to know what the mean, standard deviation and shape of the sampling distribution of the sample proportion is, three conditions must be checked and met. List each condition, and briefly comment on whether or not each condition is met in this case.

Condition 1 is:

Is condition 1 met? (Circle one): Yes No Briefly explain your answer:

Condition 2 is:

Is condition 2 met? (Circle one): Yes No Briefly explain your answer:

Condition 3 is:

Is condition 3 met? (Circle one): Yes No Briefly explain your answer:

Question 8 (continued):

- iii) (6 points) Regardless of your answers above, assume the appropriate conditions are met. What is the (a) mean, (b) standard deviation and (c) shape of the sampling distribution of the sample proportion in this case?

a) = _____

b) = _____

c) = _____

- iv) (2 points) Suppose that after 10 years pass, she finds that 16 of the 50 water heaters still work. Calculate the sample proportion.

- v) (3 Points) Using your answers from parts (iii) and (iv), calculate the z-score for this observation.

[Note: if you have no answers for part (iii) and/or part (iv), make up answers for those parts here, and use those values to answer this question.]

- vi) (4 points) Given your answer to part (v), would you consider having 16 or more out of 50 Always Hot brand water heaters still working after 10 years an “unusual” event?

Circle one: YES NO

Briefly explain your “yes” or “no” choice below. Limit your answer to two or less sentences.

9. Suppose one takes many, many repeated random samples of size $n=50$ from a very large population (of quantitative observations) that is slightly skewed right, has a mean of 127.5 and a standard deviation of 28.5.

i) (2 points) What would be the average of the sampling distribution of the sample mean?

ii) (2 points) What would be the standard deviation of the sampling distribution of the sample mean?

iii) (2 points) Assume all the of necessary conditions are met for the Central Limit Theorem to apply to the sampling distribution of the sample mean (which, they ARE met in this case). Given that the Central Limit Theorem applies, what would be the shape of the sampling distribution of the sample mean?

iv) (6 points) In one particular sample of $n=50$, a sample mean of 150.7 was obtained. Would you consider this to be a “rare” or “unusual” value of the sample mean? Use your answers above to help you answer this question. Provide whatever arithmetic you need to help you answer this question, and be sure to show your work.

Circle one: “rare event” “not a rare event”

Briefly justify the choice you circled above. Limit your answer to two or less sentences.

(NOTE 1: If you have NO answers to parts [i] and/or [ii], make up answers for those parts here, and use that to answer this question. **NOTE 2:** If you have a calculator that can calculate the probability of this event, do NOT use that capability!)

True/False
Circle the best answer
(2 points each)

- T F Extrapolation occurs when someone uses a linear regression model to make a prediction outside the original scope of the independent variable, x .
- T F Event A is “a randomly selected student from Brian’s class makes an A in Stat 201”. Event B is “a randomly selected student from Brian’s class is a sophomore”. Events A & B are mutually exclusive events.
- T F If Event A and Event B are independent, knowing the outcome of Event A changes the probability of Event B occurring.
- T F Stratified Random Sampling occurs when the researcher picks a random starting point, and then samples every k th element or observation from the sampling frame.
- T F Two events that are independent must have equal probabilities of occurring.
- T F Comment cards at a restaurant are an example of convenience sampling.